

ROTATION & TORQUE

Tangential Velocity

$$\bullet V_T = \frac{d}{t} = \frac{2\pi r}{T}$$

- Distance = circumference
- Time = period

Equilibrium

- Forces must be balanced in the x and y directions.

- But for rotation:

“Clockwise torques must be equal to counter-clockwise torques.”

- $\tau = F \times r$

- Example...

Angular Momentum

- Just like bodies have linear momentum $p=mv$, they have angular momentum:

$$\mathbf{L} = \mathbf{I}\boldsymbol{\omega}.$$

- I is the object's moment of inertia (the rotational version of mass).
- ω is the angular velocity, where $\omega=2\pi r$ and is measured in rad/s.
- L is measured in $\text{kg m}^2 / \text{s}$

Conservation of L

Angular momentum, just like regular momentum, is always conserved in a closed system.

Angular Momentum

- An object with angular momentum tends to keep moving, unless the torques become unbalanced.
- Just like how an object with linear momentum tends to keep moving.

Angular Momentum

- For a point mass undergoing circular motion:

$$\mathbf{L} = m\mathbf{v}r$$

where m is the mass of the object
 v is the tangential velocity,
 r is the radius of the circle